(12)

### SECTION - B

2

3. Using the Bellman's principle of optimality,

Minimize  $Z = y_1 + y_2 + y_3 + \dots + y_n$ 

subject to  $y_1.y_2.y_3.....y_n=b$ ,

 Find the basic feasible solution of the following transportation problem by north west corner rule. Also find the optimal transportation plan.



5. Consider the following function:

 $f(X) = 5x_1 + 2x_2^2 + x_3^2 - 3x_3x_4 + 4x_4^2 + 2x_5^4 + x_5^2 + 3x_5x_6 + 6x_6^2 + 3x_6x_7 + x_7^2$ 

Show that f(x) is a convex by expressing it as a sum of functions of one or two variables and then proving that all the functions are convex. (12)

17033(M)

B. Tech 4th Semester Examination

**Optimization and Calculus of Variations (CBS)** 

MA-401

Time : 3 Hours

#### Max. Marks : 60

(6)

The candidates shall limit their answers precisely within the answerbook (40 pages) issued to them and no supplementary/continuation sheet will be issued.

**Note :** Attempt five question in all, selecting one question from each Sections A, B, C and D. Section E is compulsory.

#### SECTION - A

1. (a) Maximize Z = 3x + 4y,

Subject to  $x-y \ge 0$ ;  $2.5x-y \le -3$ ;  $x, y \ge 0$ 

By graphical method.

- (b) Why do some problems have multiple optimal feasible solutions? What is the effect of changing the objective function on the optimum point? Discuss.
   (6)
- Use simplex method to solve the following problem:

Maximize Z =  $4x_1 + 3x_2 + 6x_3$ , subject to  $2x_1 + 3x_2 + 2x_3 \le 440$ ,  $4x_1 + 3x_3 \le 470$ ,  $2x1 + 5x_2 \le 430$ ,  $x_1, x_2 \ge 0$  (12)

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The time estimates (in weeks) for the activity of a PERT network are given below:

Activity	t <sub>o</sub>	t <sub>m</sub>	tp
1-2	1	1	7
1-3	1	4	7
1-4	2	2	8
2-5	1	1	1
3-5	2	5	14
4-6	2	5	8
5-6	3	6	15

- (a) Draw the project network and identify all the paths through it.
- (b) Determine the expected project length.
- (c) Calculate the standard deviation and variance of the project length.
- (d) What is the probability that the project will be completed at least 4 weeks earlier than the expected time?
- (e) If the project due date is 19 weeks, what is the probability of not meting due date?
- (f) The probability that the project will be completed on the schedule if the schedule completing time is 220 weeks. (12)

## SECTION - D

- (a) Find the plane curve of fixed perimeter and maximum area.
  (6)
  - (b) Find the extremals of the following functionals:

×

$$\int_{0}^{\frac{\pi}{2}} (y^{2} - y'^{2} - 2y \sin x) dx; \ y(0) = y\left(\frac{\pi}{2}\right) = 0.$$
 (6)

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8. (a) Show that the geodesics on a sphere of radius a are its great circles. (6)

(b) Find a function y(x) for a function for which 
$$\int_{0}^{0} (x^{2} + {y'}^{2}) dx$$
  
is stationary, given that  $\int_{0}^{1} y^{2} dx = 2$ ; y(0)=0, y(1)=0. (6)  
SECTION - E

- 9. Attempt all the questions:
  - (a) Give the advantages of network models.
  - (b) Write the two difficulties in using network models.
  - (c) Give short note on restrictions on assignments.
  - (d) Write short note on degenerate transportation problem.
  - (e) Define the term alternate courses of action.
  - (f) Explain the term SLACK variables with example.
  - (g) State two rules to avoid cycling.
  - (h) Define functionals of a calculus of variation.
  - (i) Find the extremals of a functional  $\int_{x_0}^{x_1} \left(\frac{y'^2}{x^3}\right) dx$ .
  - Define convexity and write its two properties.
  - (k) What are the advantages of duality theory?
  - Define dynamic programming for Bellman's Principle of optimality.
     (1×12=12)